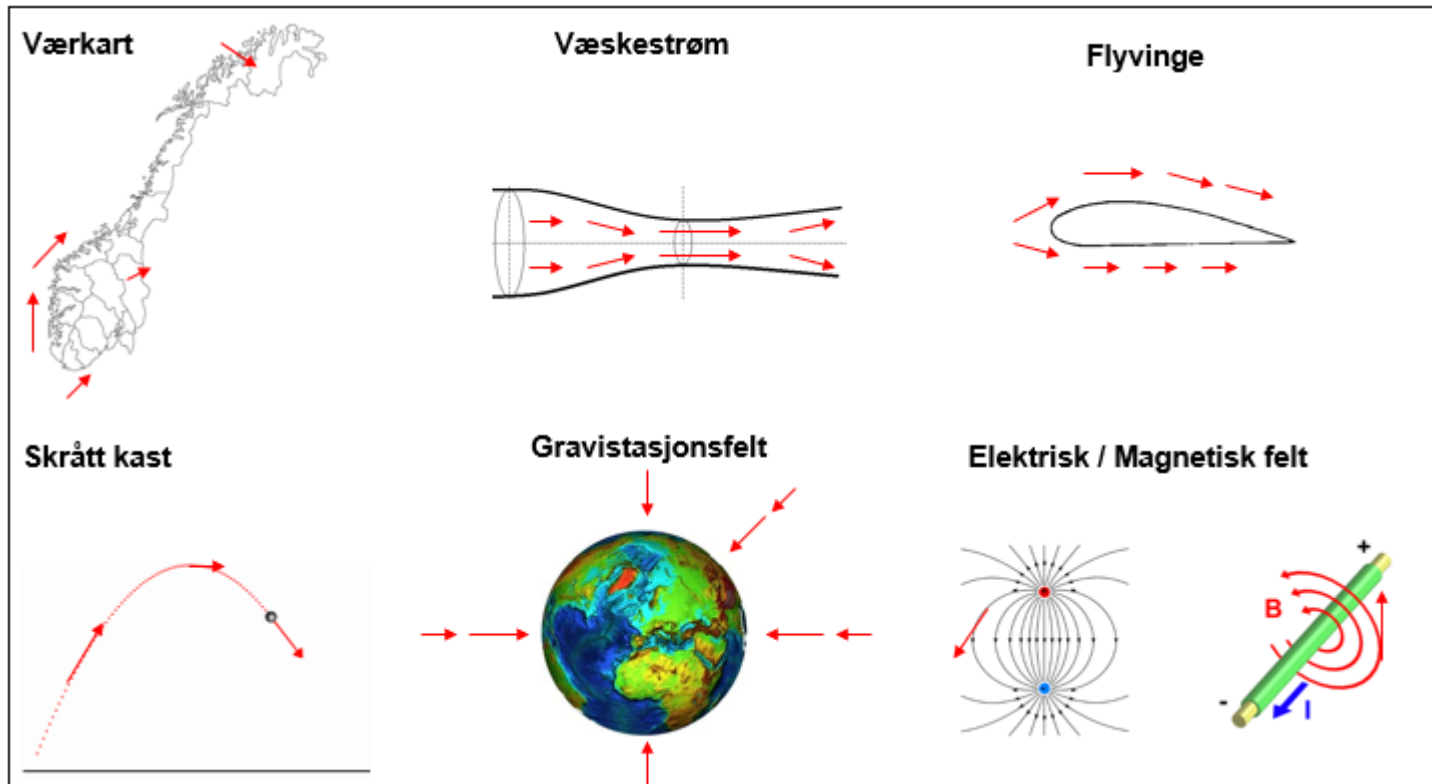
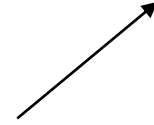


# Vektor

En vektor er et objekt som er karakterisert ved en lengde og en retning

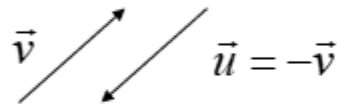


## Vektor

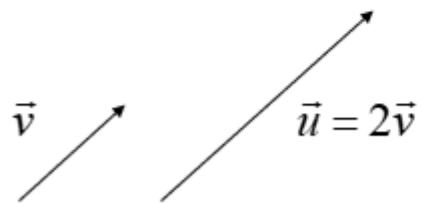
### Likhet og multiplikasjon med skalar



**Samme lengde og samme retning**



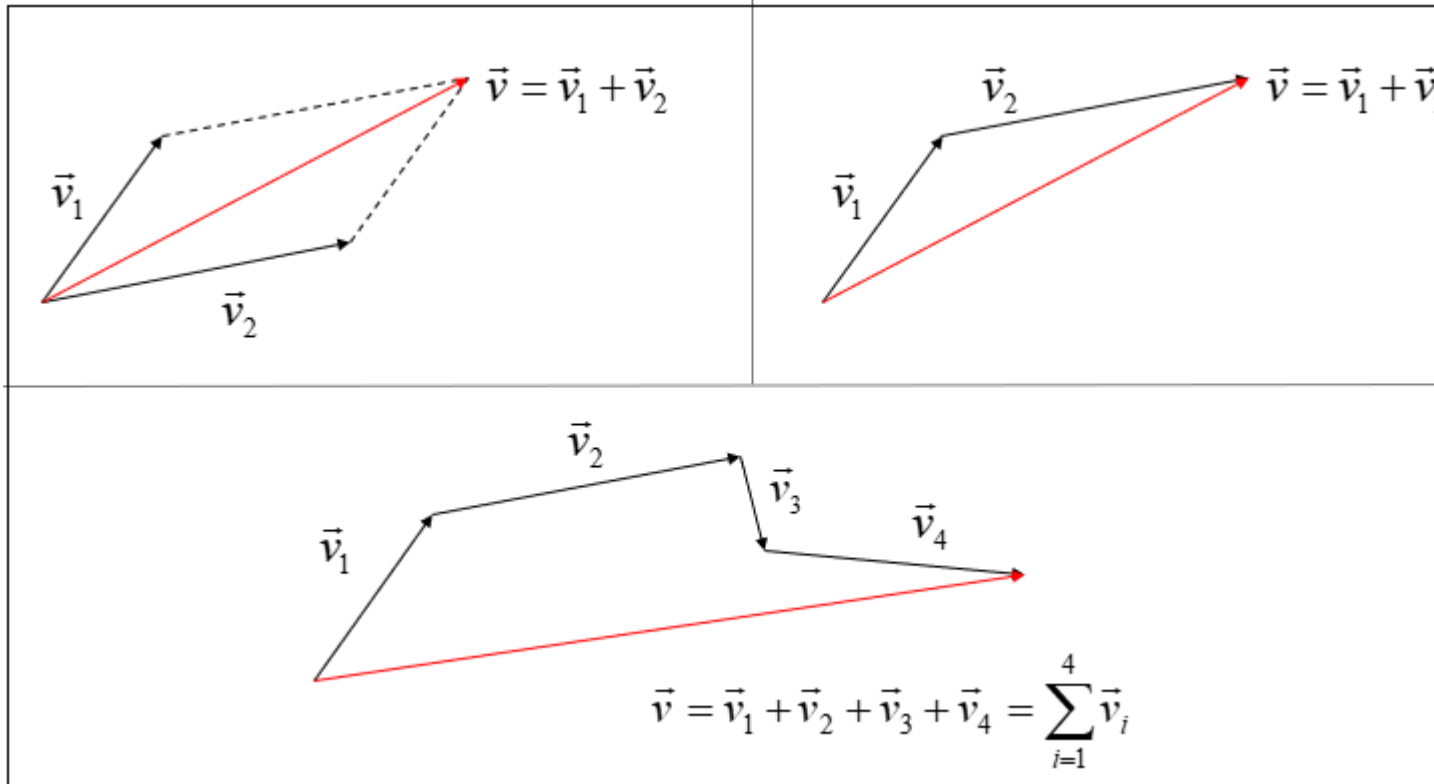
**Samme lengde og motsatt retning**



**Dobbel lengde og samme retning**

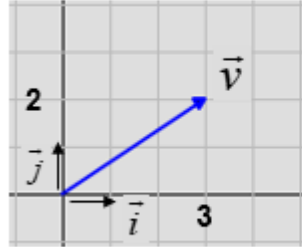
# Vektor

## Addisjon



# Vektor

## Notasjon



$$\begin{aligned}\vec{v} &= 3\vec{i} + 2\vec{j} \\ &= [3, 2] \\ &= \begin{bmatrix} 3 \\ 2 \end{bmatrix}\end{aligned}$$

## Skalarprodukt

$$c = \vec{v}_1 \cdot \vec{v}_2 = |\vec{v}_1| \cdot |\vec{v}_2| \cdot \cos \alpha$$

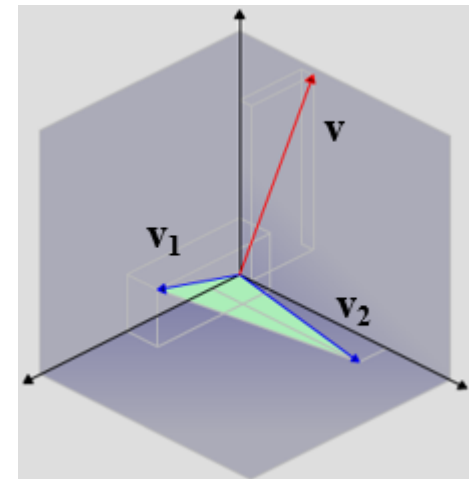
$$c = \vec{v}_1 \cdot \vec{v}_2 = [v_{1x}, v_{1y}, v_{1z}] \cdot [v_{2x}, v_{2y}, v_{2z}] = v_{1x} \cdot v_{2x} + v_{1y} \cdot v_{2y} + v_{1z} \cdot v_{2z}$$

## Kryssprodukt

$$|\vec{v}| = |\vec{v}_1 \times \vec{v}_2| = |\vec{v}_1| \cdot |\vec{v}_2| \cdot \sin \alpha$$

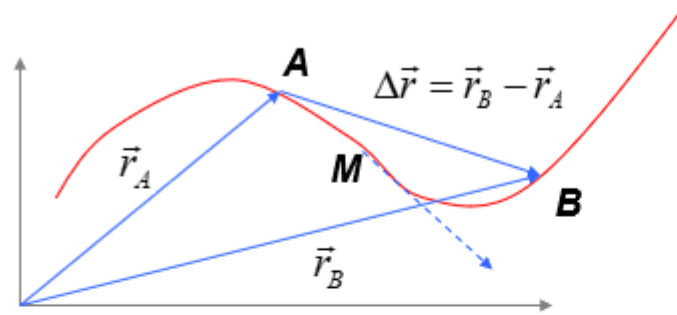
$$[\vec{v}] = \vec{v}_1 \times \vec{v}_2 = [v_{1x}, v_{1y}, v_{1z}] \times [v_{2x}, v_{2y}, v_{2z}]$$

$$= [v_{1y}v_{2z} - v_{1z}v_{2y}, v_{1z}v_{2x} - v_{1x}v_{2z}, v_{1x}v_{2y} - v_{1y}v_{2x}]$$



# Vektor

## Derivasjon



**Gjennomsnittshastighet på strekningen A-B:**

$$\bar{v} = \frac{\Delta \vec{r}}{\Delta t}$$

**Hastighet (momentanhastighet) i M:**

$$\bar{v} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{r}}{\Delta t} = \frac{d\vec{r}}{dt} = \dot{\vec{r}}$$